



# AN ATYPICAL JOINT MODEL OF PSA AND CTC COUNT KINETICS DURING TREATMENT IN PROSTATE CANCER

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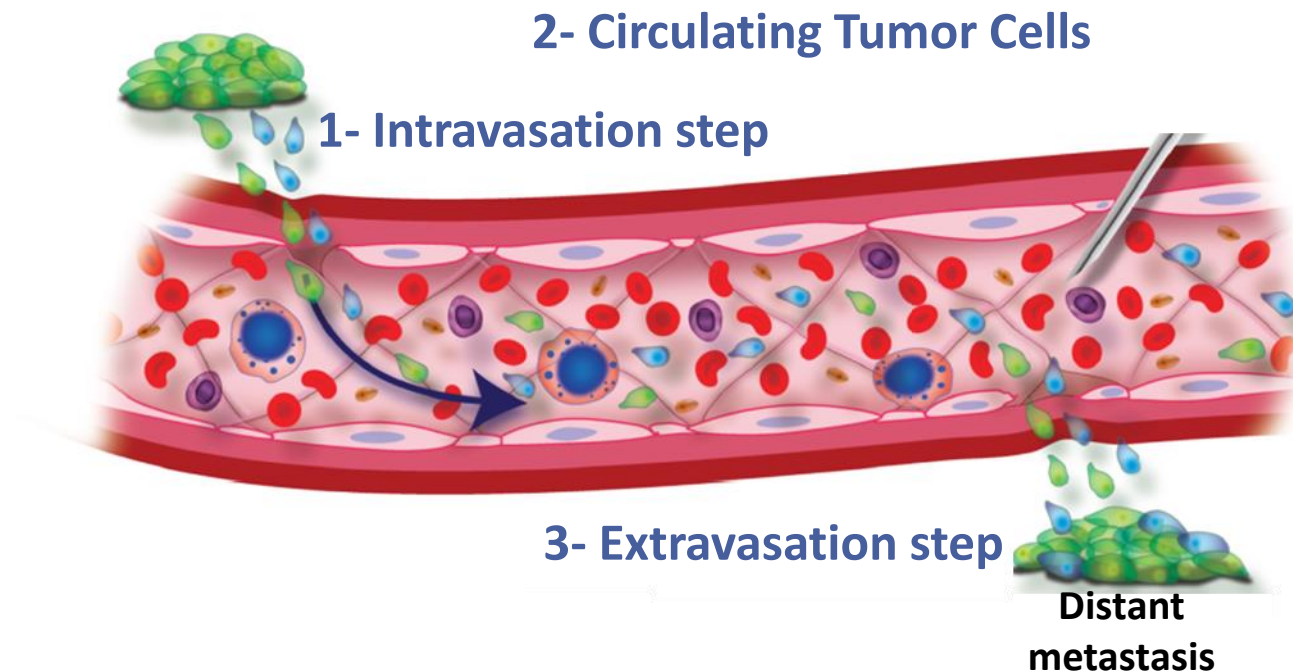
# BACKGROUND

# Background – Prostate cancer & PSA

- **Prostate cancer (PC):**
    - The most common cancer
    - The 3<sup>rd</sup> leading cause of cancer deaths
    - Bone: the most common site of metastasis → non-measurable tumor burden / disease evolution to evaluate treatment efficacy
  - **PSA (Prostate-Specific Antigen):**
    - The most widely used serum tumor marker to evaluate treatment effect in PC
    - Controversial validity of its use as a surrogate marker
- **Need of strong surrogate markers for disease outcome and clinical benefit in metastatic PC**

# Background – CTCs: Definition

- Circulating Tumor Cells <sup>1</sup>: new emergent serum tumor marker
- Tumor cells released into blood which potentially lead to the development of metastases <sup>2</sup> :



<sup>1</sup> Ashworth et al. A case of cancer in which cells similar to those in the tumours were seen in the blood after death. *The Medical Journal of Australia*. 1869. <sup>2</sup> Danila et al. Circulating tumor cells as biomarkers. *Cancer J*. 2011.

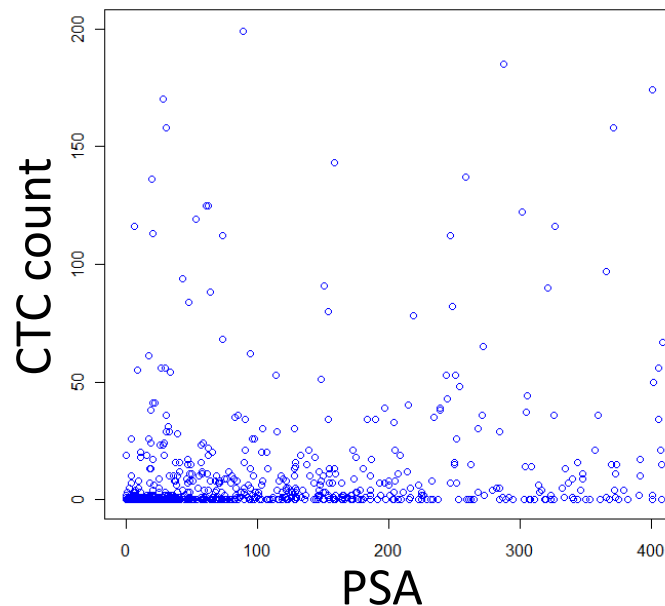
# Background – CTCs: Definition

- Circulating Tumor Cells <sup>1</sup>: new emergent serum tumor marker
  - Tumor cells released into blood which potentially lead to the development of metastases <sup>2</sup> :
- Potential application as a **biomarker** in oncology
  - In PC: CTC count (<5 vs ≥5) associated with **overall survival** <sup>3</sup>
  - CTC count **better predictor** of survival than PSA decrease <sup>3</sup>

<sup>3</sup> De Bono et al. Circulating tumor cells predict survival benefit from treatment in metastatic castration-resistant prostate cancer. *Clin Cancer Res.* 2008.

# Background – CTC count kinetics

- Could be a useful tool to evaluate treatment response
  - Could provide information about the evolution of the total tumor burden = primary tumor + metastases
- **Kinetics of CTC counts, along with their relationships with other markers, need to be addressed**



- No clear direct relationship
- Different kinetics

# Objectives

- To quantify the **dynamic relationships** between the kinetics of PSA and CTC count in metastatic prostate cancer patients under treatments
- To build a semi-mechanistic model combining several **advanced features** in pharmacometrics

# PATIENTS & METHODS



# Patients & Data

- **223** metastatic castration-resistant prostate cancer (mCRPC) patients <sup>3</sup>
- Treated by chemotherapy + / - hormonotherapy
- For each patient:
  - No drug concentration data
  - **Number of CTCs / 7.5 mL aliquot** of blood : Med = 2 [0 – 6 437] (CellSearch method)
  - **PSA concentration** (ng.mL<sup>-1</sup>) : Med = 116 [LOQ – 17 800]
  - Median of **4** PSA and **4** CTCs values per patient

<sup>3</sup> De Bono et al. Circulating tumor cells predict survival benefit from treatment in metastatic castration-resistant prostate cancer. *Clin Cancer Res.* 2008.

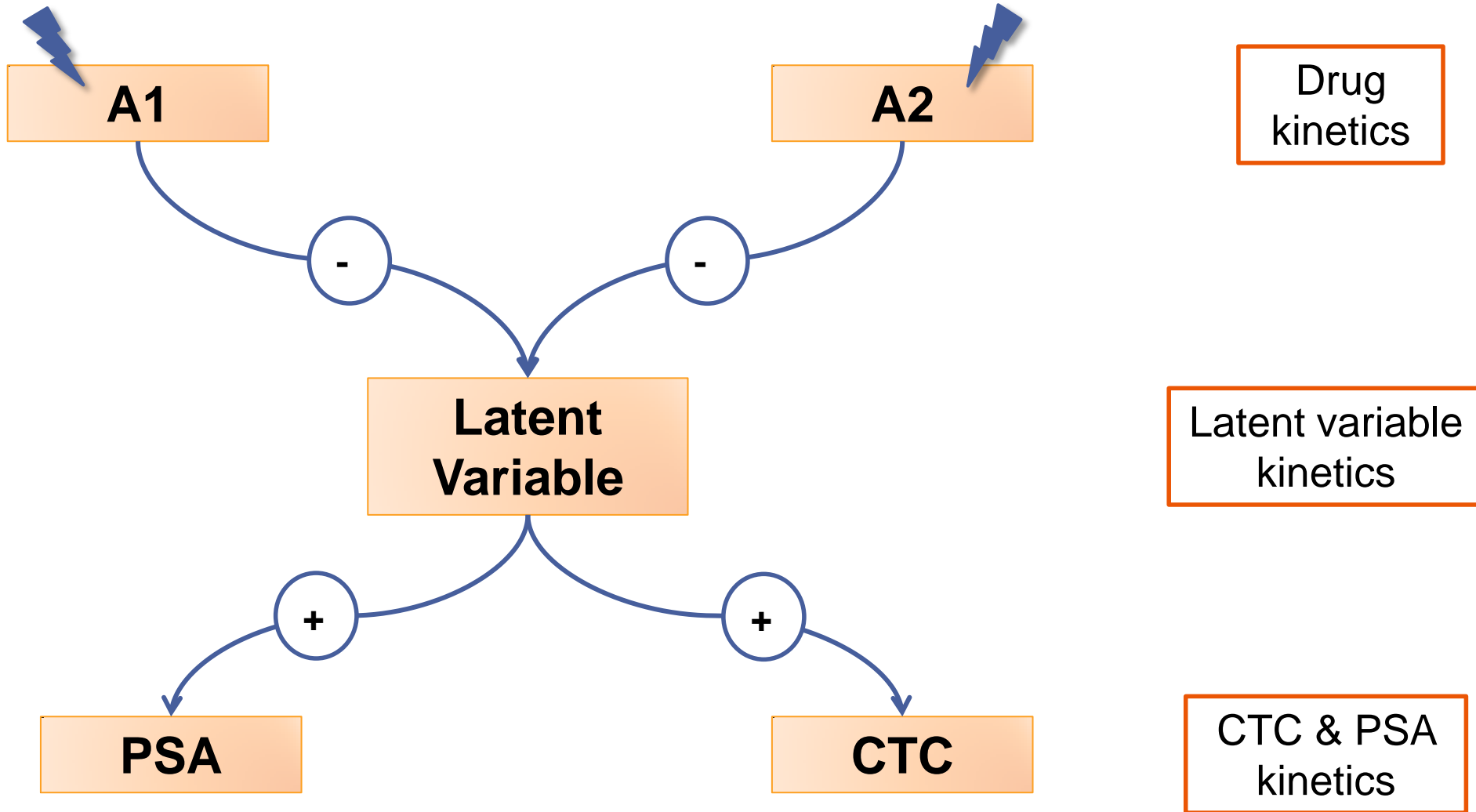
# Modeling Methods

- Model-building process:
  - Model for PSA kinetics
  - Model for CTC count kinetics
  - Combined and linked with a **common unobserved variable**
- **Non-linear mixed effects** modeling:
  - NONMEM 7.3 (SAEM algorithm)
  - Model selection & evaluation:
    - Likelihood
    - Standard error (SE) and Shrinkage values
    - Goodness-of fit (GOF) plots
    - Simulation-based diagnostics (Visual predictive Check: VPC)

# MODEL STRUCTURE

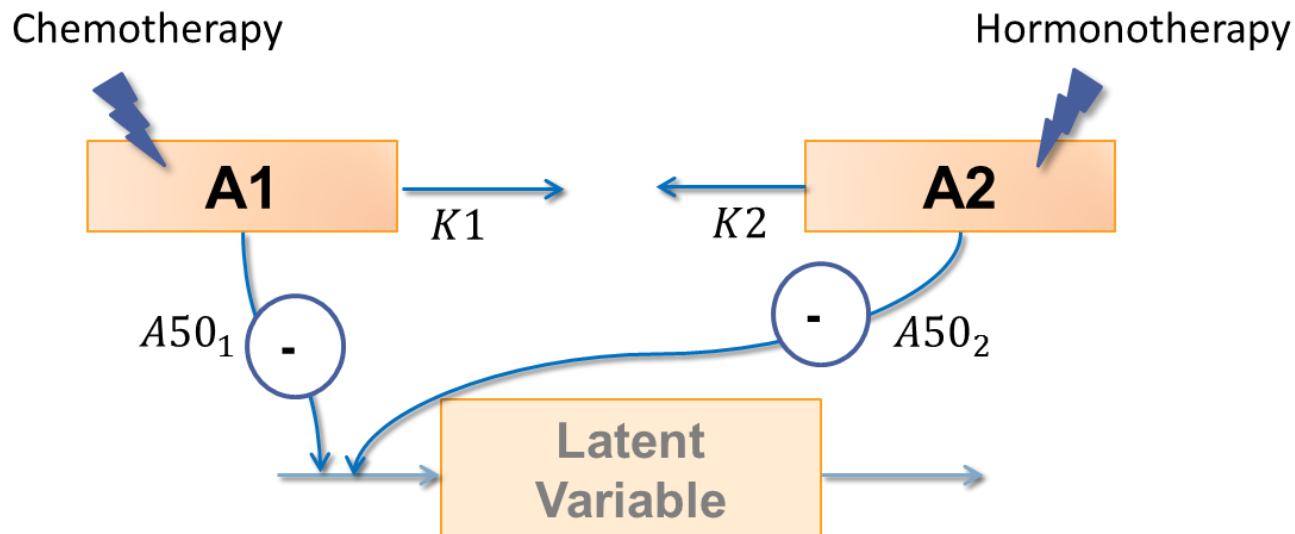
Chemotherapy

Hormonotherapy



# Drug effect kinetics

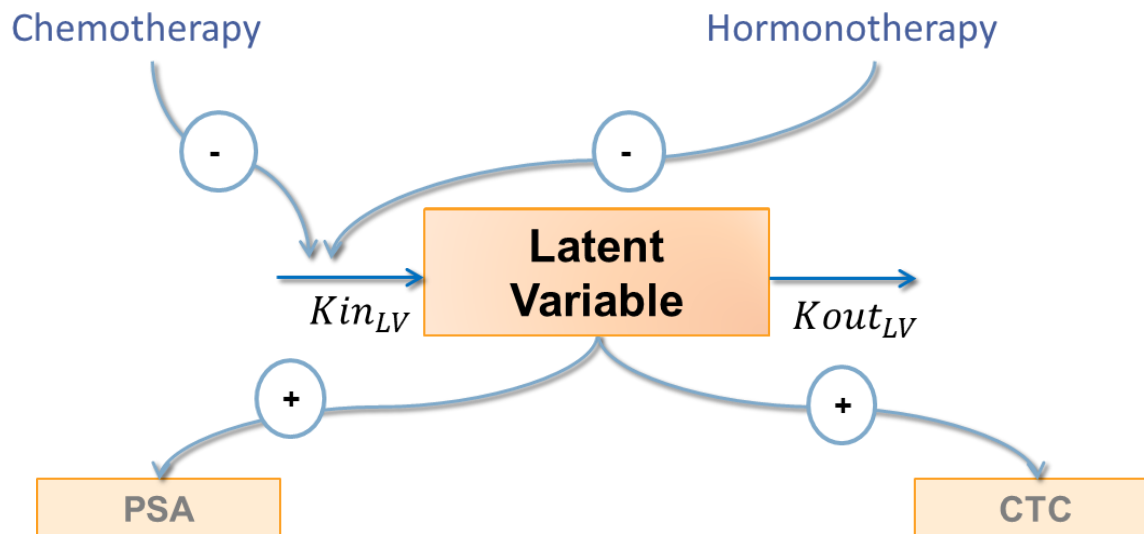
- No PK data → **K-PD** approach <sup>4</sup>
- 2 K-PD compartments for chemotherapy and hormonotherapy
- Estimation of different kinetics and efficacy parameters



<sup>4</sup> Jacqmin et al. Modelling response time profiles in the absence of drug concentrations: definition and performance evaluation of the K-PD model. *J Pharmacokinet Pharmacodyn.* 2007.

# Dynamic links between PSA and CTC

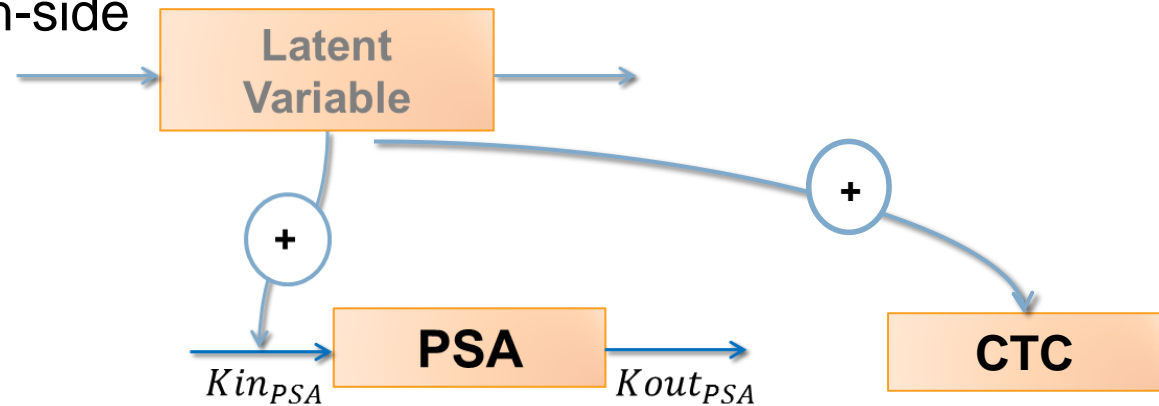
- No clear direct relationship, but triggered by a common variable
- Use of a **latent variable**: underlying, non-observed variable
  - Non-steady-state model
  - 0-order production and 1<sup>st</sup> order elimination rates



# Joint modeling of PSA and CTC kinetics

- **PSA:**

- **Continuous** data
- Non-steady-state model
- 0-order production and 1<sup>st</sup> order elimination rates
- Log-transformed both-side



- **CTC count:**

- **Discrete** data
- Produced by a discrete process
- **Cell Life Span model** <sup>5</sup>

<sup>5</sup> Krzyzanski et al. Lifespan based indirect response models. *J Pharmacokinet Pharmacodyn.* 2012.

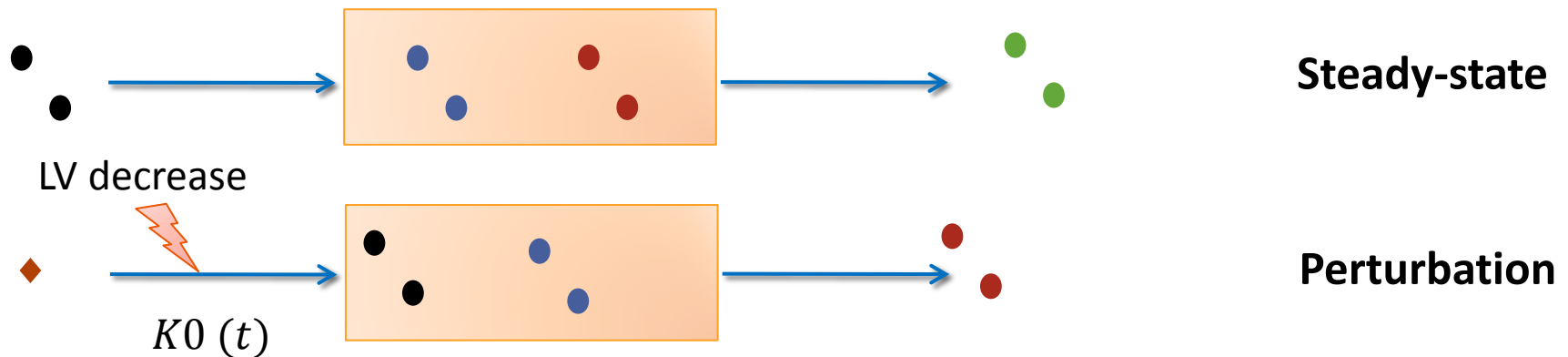
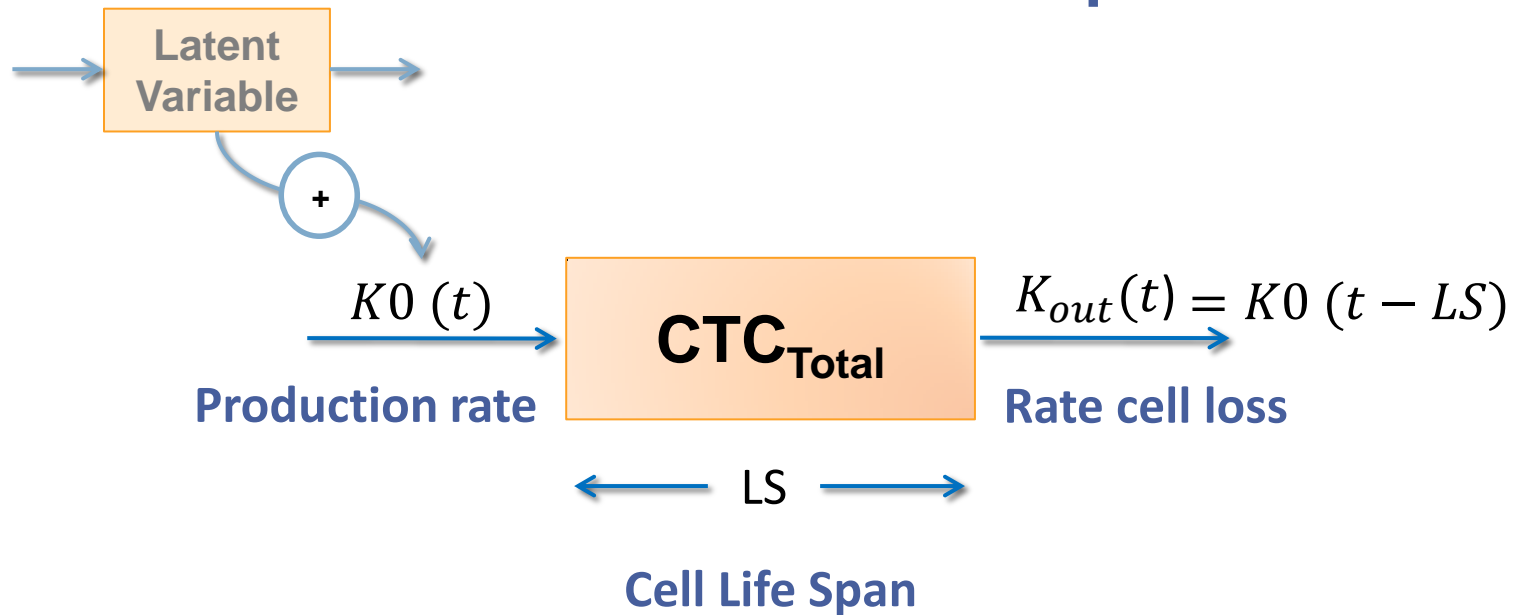
# CTC kinetics: Cell Life Span model

- Commonly used for the modeling of blood cells maturation <sup>5</sup>

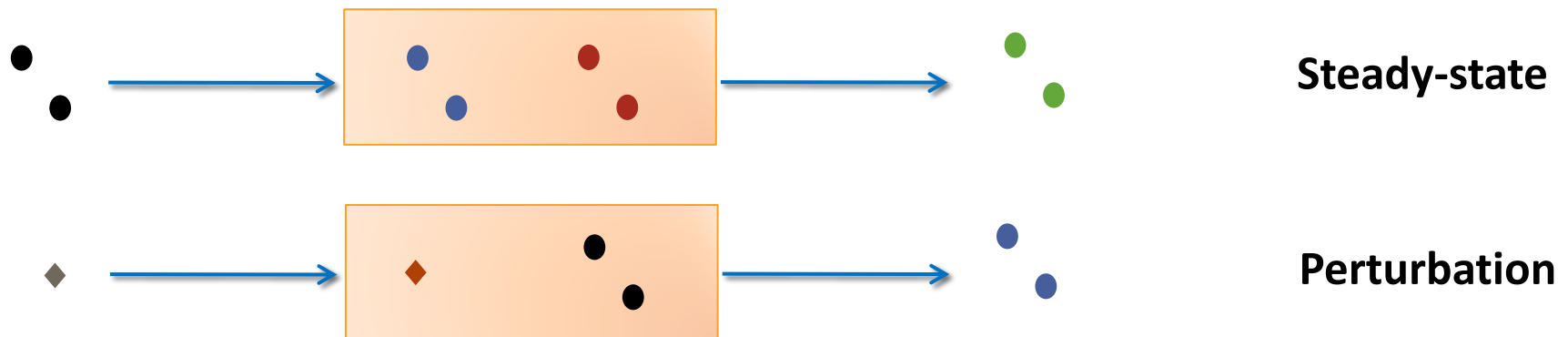
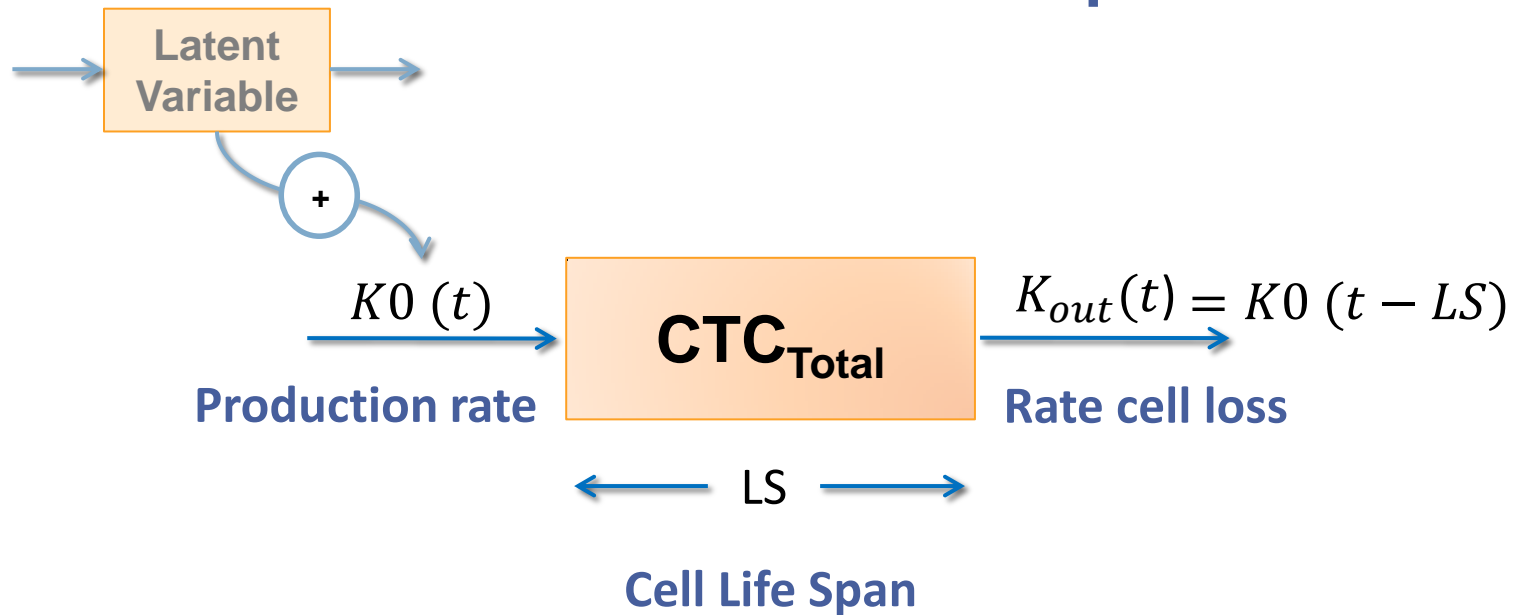
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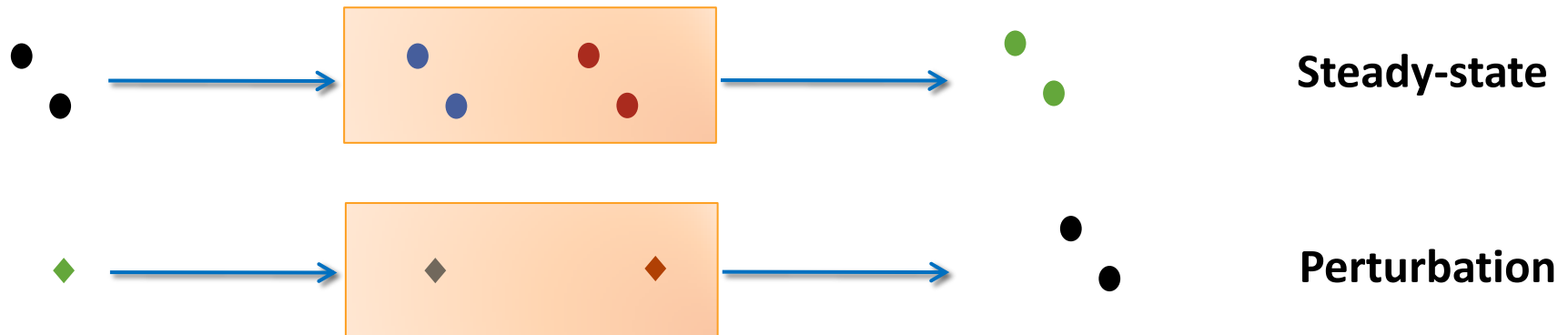
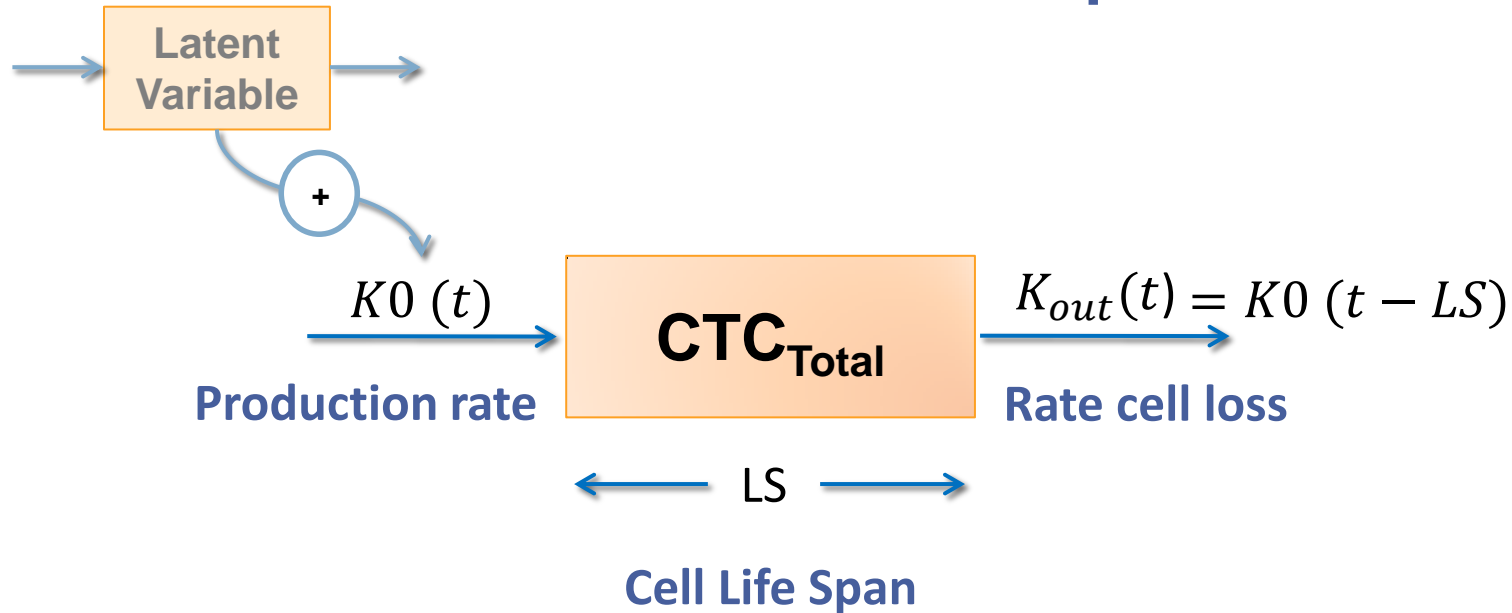
# CTC kinetics: Cell Life Span model



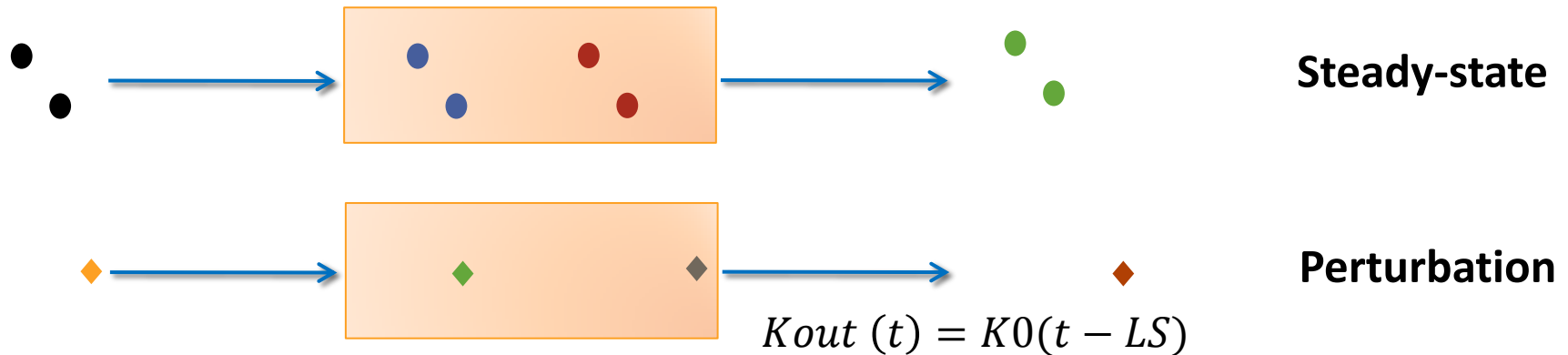
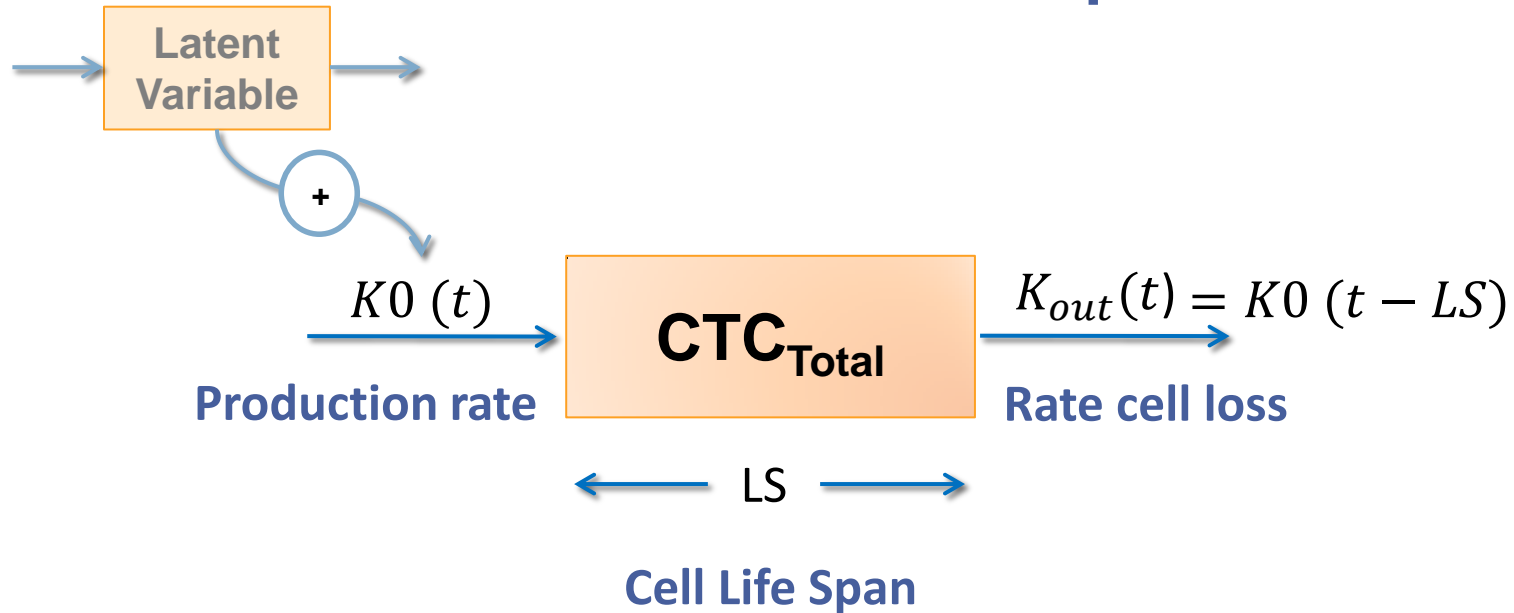
# CTC kinetics: Cell Life Span model



# CTC kinetics: Cell Life Span model

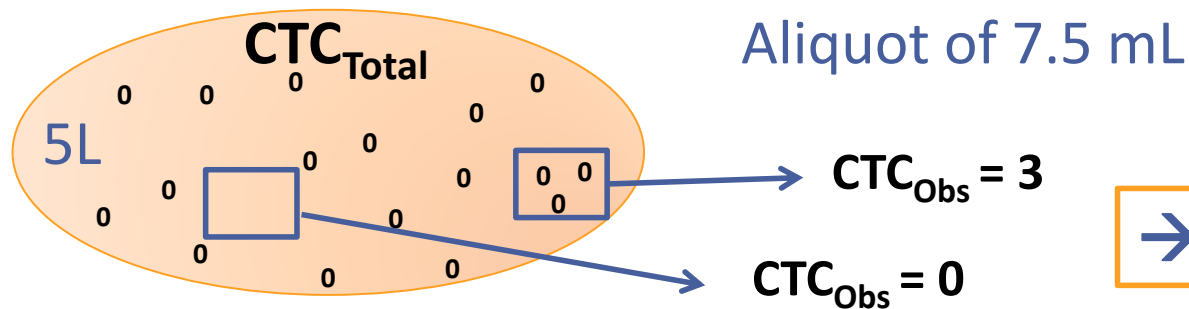


# CTC kinetics: Cell Life Span model



# Random sampling of CTCs

- The observed CTC count is a sample of a true CTC count:



→ Random process

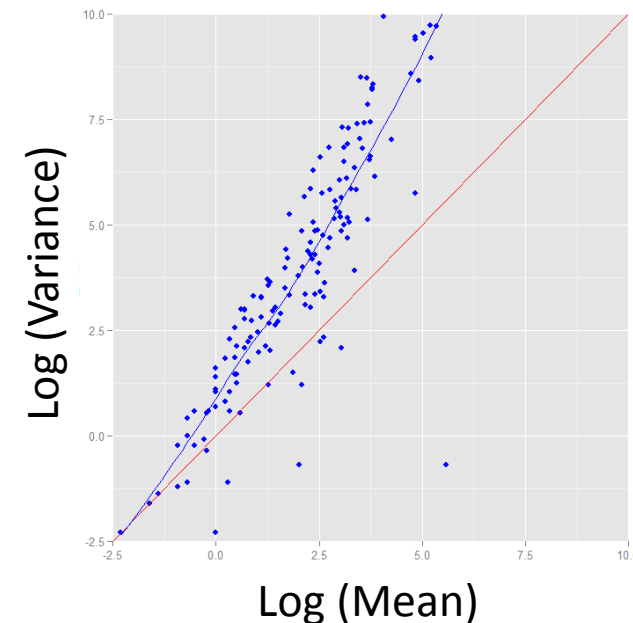
- Expected CTC count per aliquot:

- Homogeneous repartition of CTCs

- $\hat{\lambda} = CTC_{Total} \times \alpha \quad \alpha = 7.5 / 5000$

- $CTC_{Obs} \sim Poisson(\lambda)$  :

- Negative Binomial distribution**
- Overdispersion: variance > mean

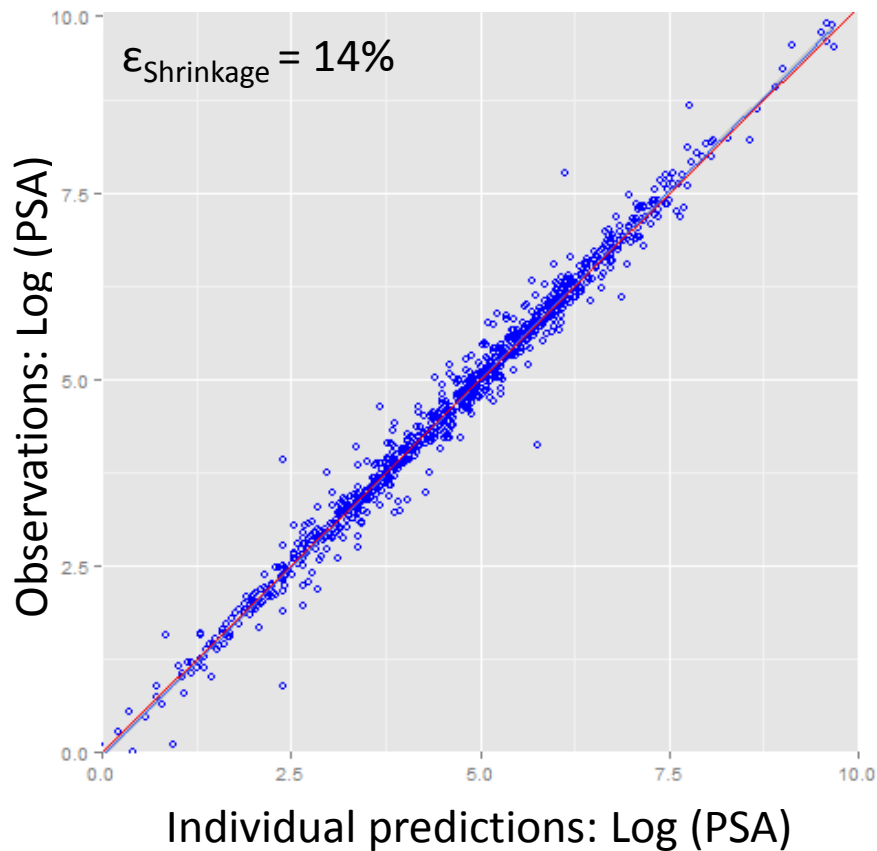


# RESULTS

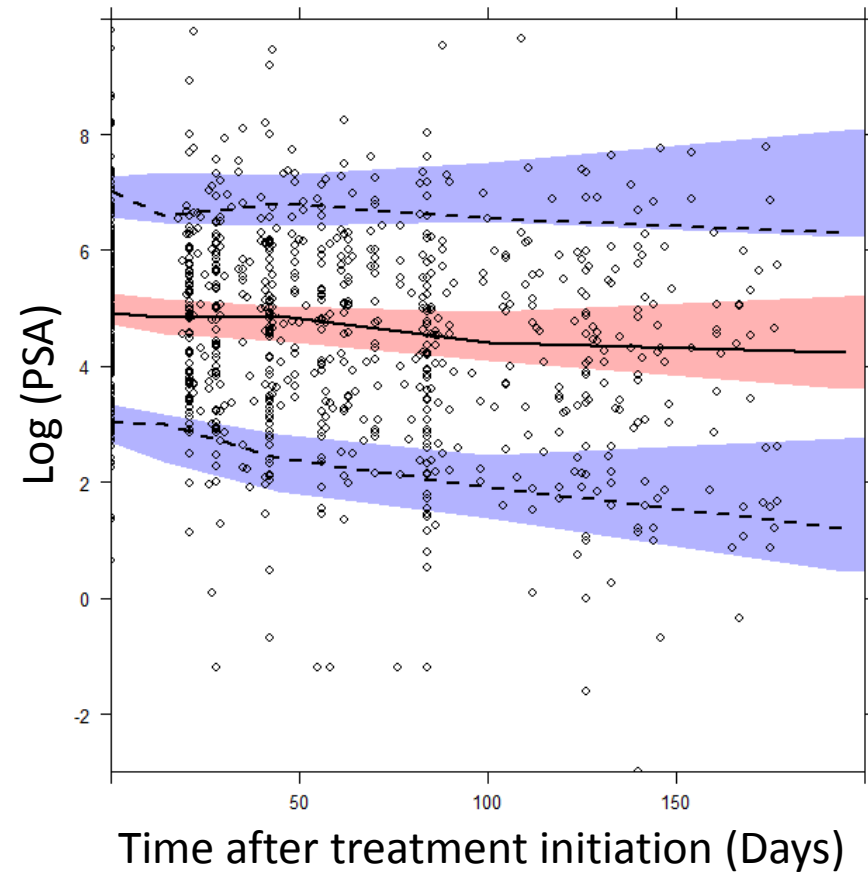
# PSA Evaluation

- ◇ Observations
- Observed percentiles
- Simulated 95% c.i of 10<sup>th</sup> & 90<sup>th</sup> percentiles
- Simulated 95% c.i of the median

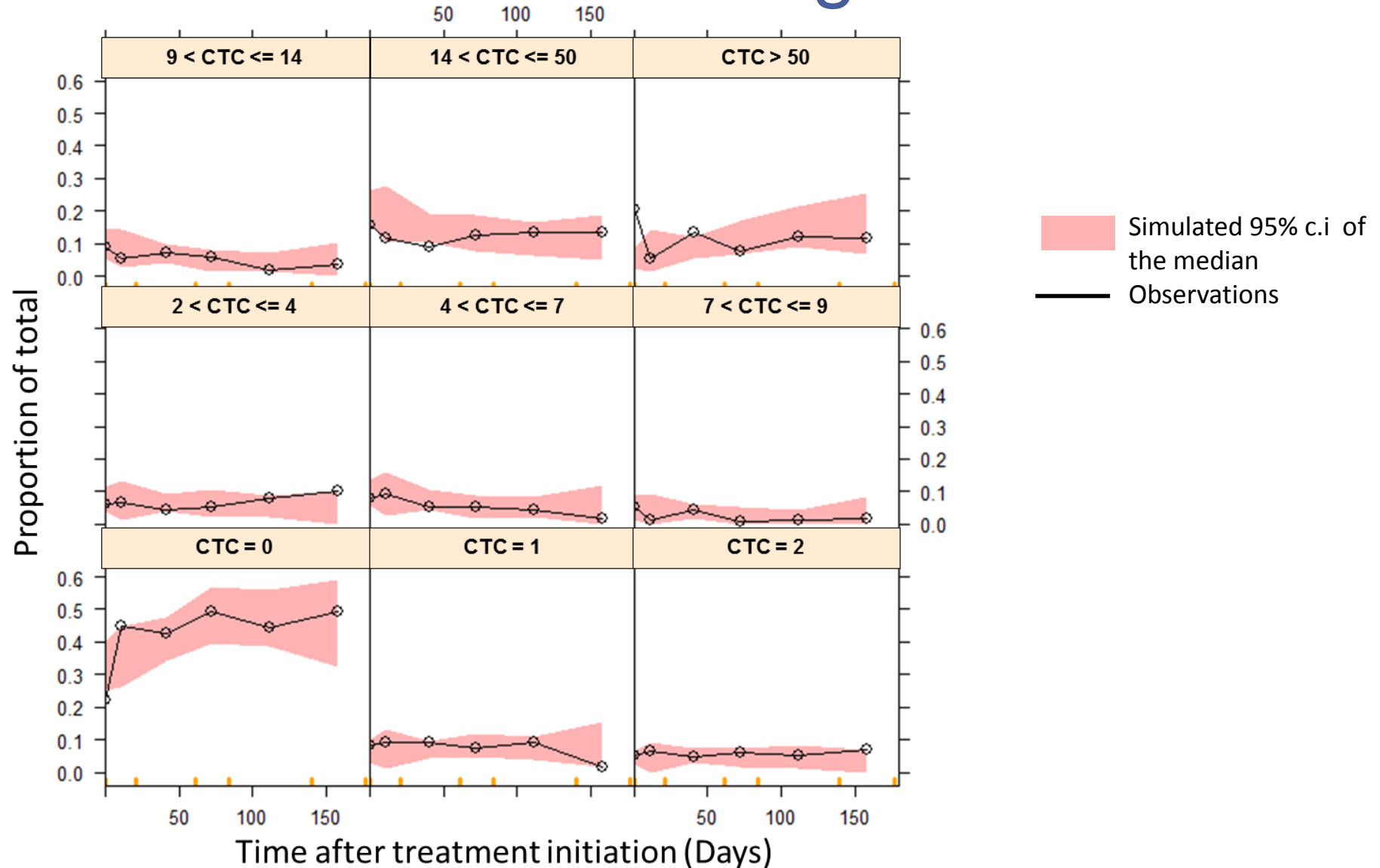
## Individual predictions VS Observations



## Visual Predictive Check (VPC)

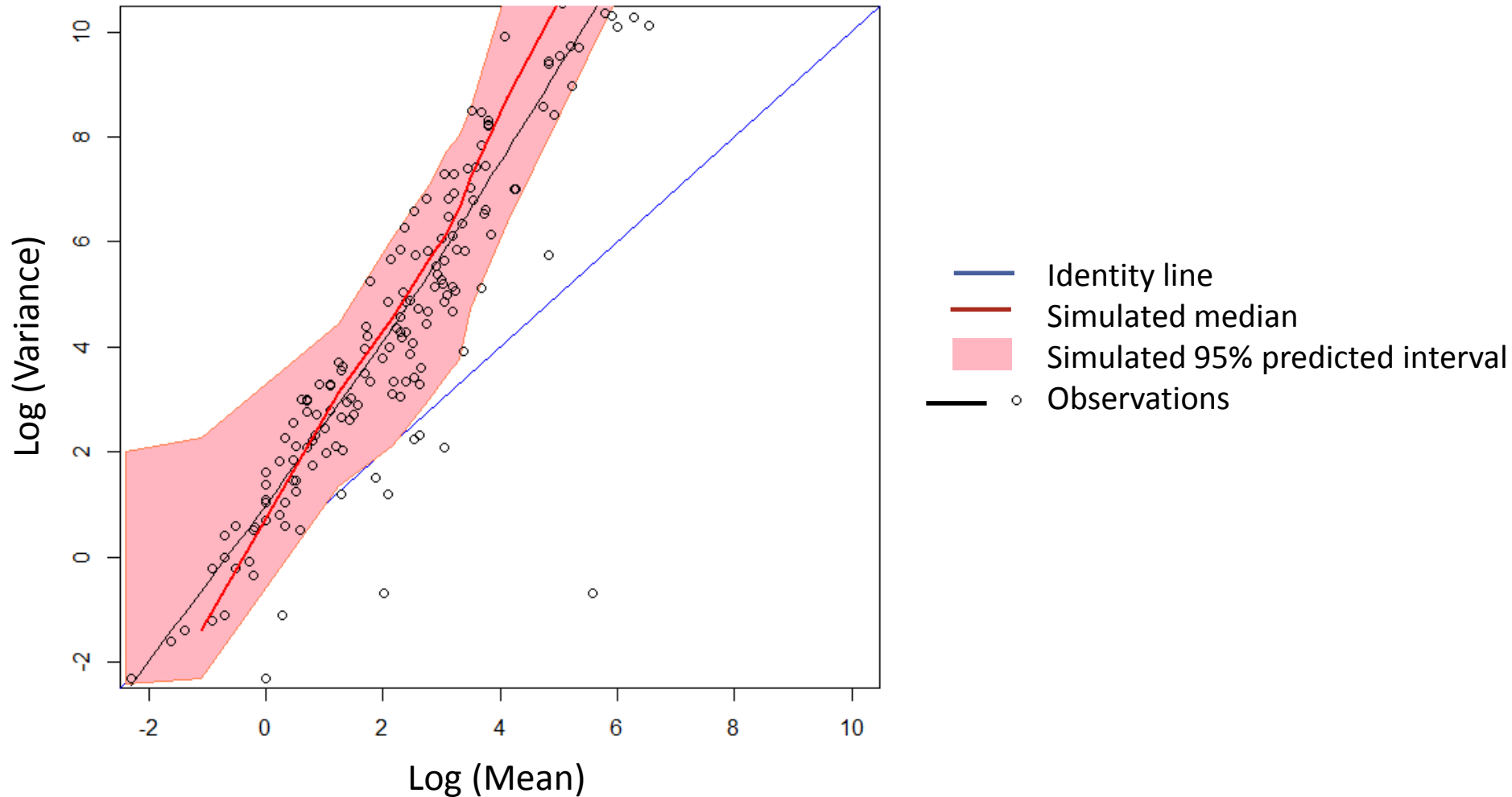


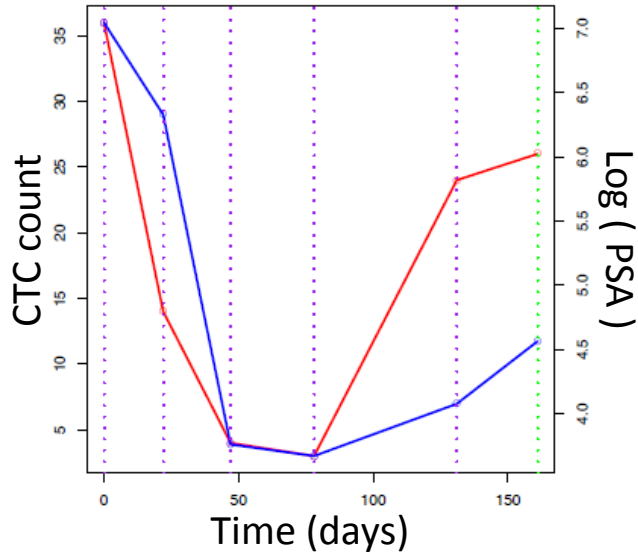
# CTC Evaluation: Categorical VPCs



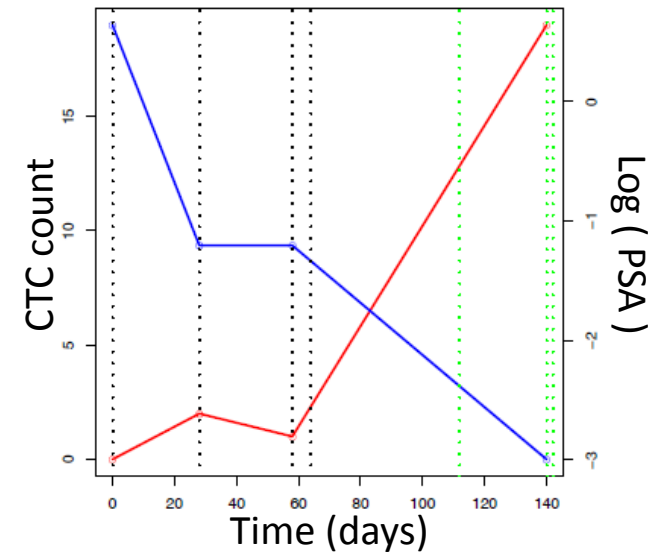


# CTC Evaluation: Overdispersion VPC



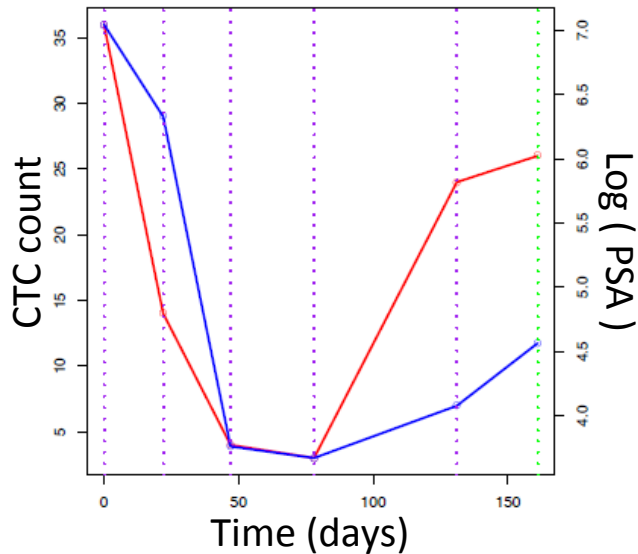
**Observed individual kinetic profile #1**

- PSA kinetics
- CTC count kinetics
- - - Chemotherapy
- - - Hormonotherapy
- - - Both treatment
- Latent variable kinetics

**Observed individual kinetic profile #2**

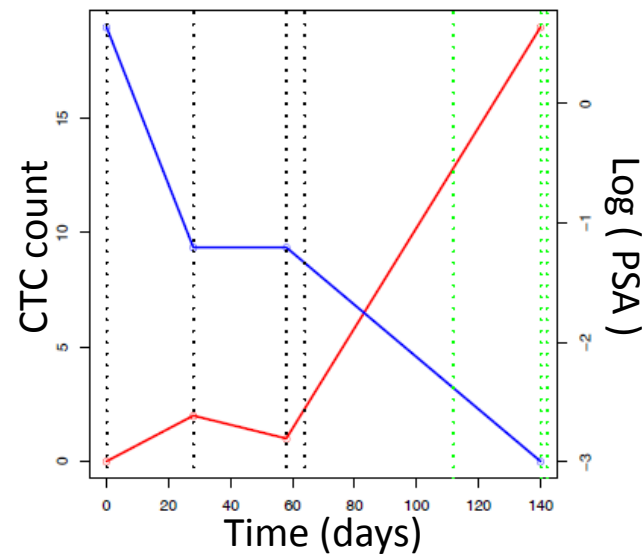
→ Large heterogeneity in the types of observed individual kinetics profiles

**Observed individual kinetic profile #1**

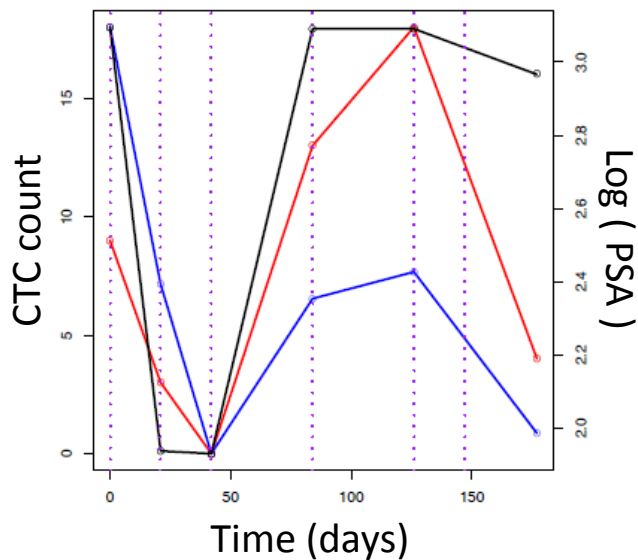


- PSA kinetics
- CTC count kinetics
- ⋯ Chemotherapy
- ⋯ Hormonotherapy
- ⋯ Both treatment
- Latent variable kinetics

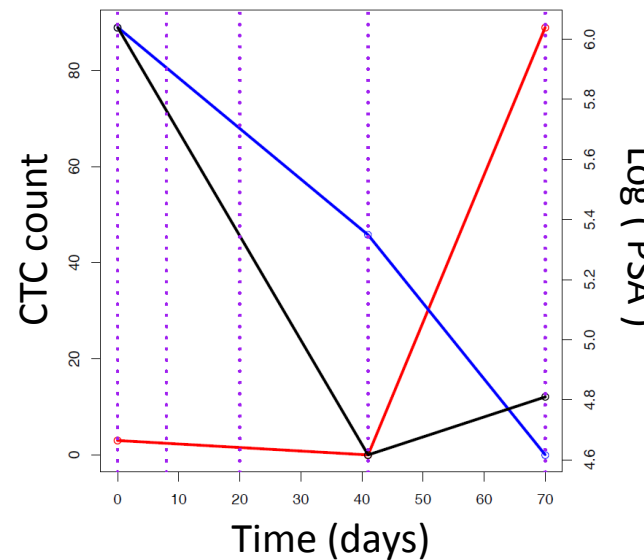
**Observed individual kinetic profile #2**

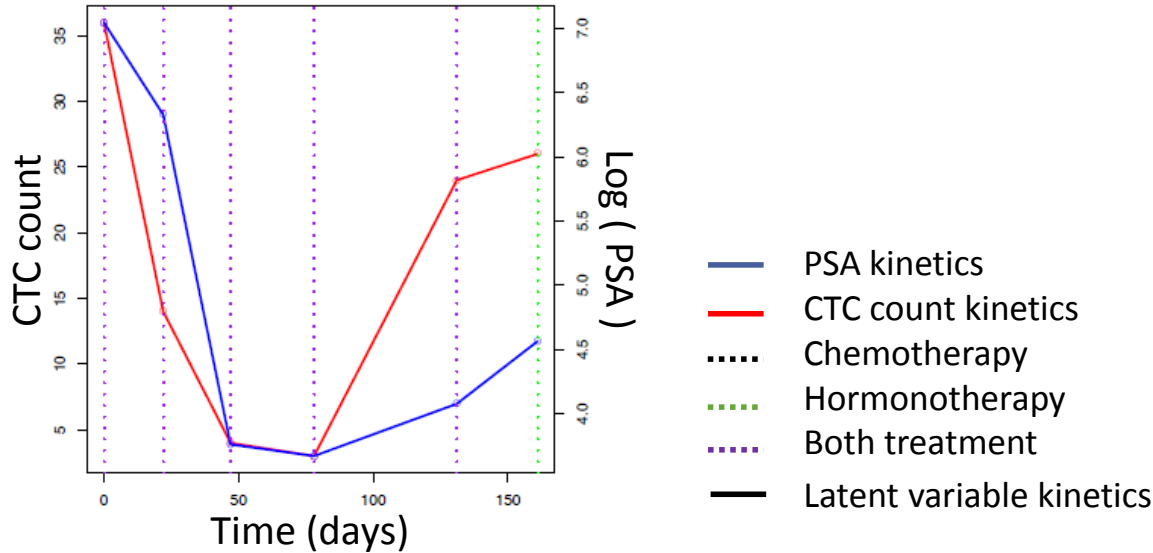
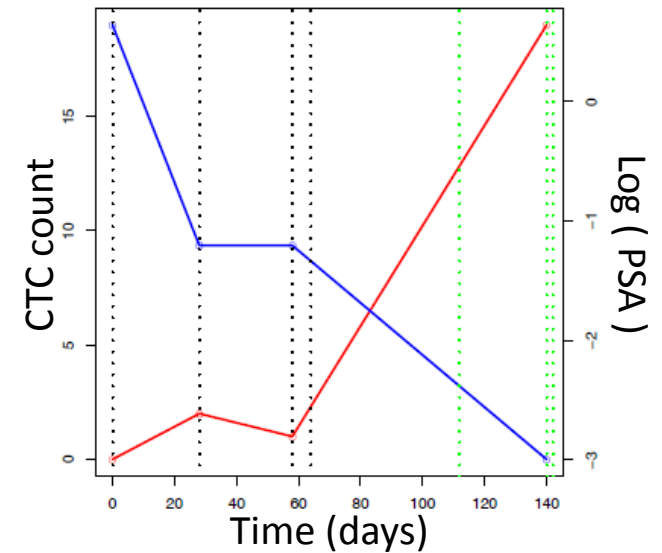
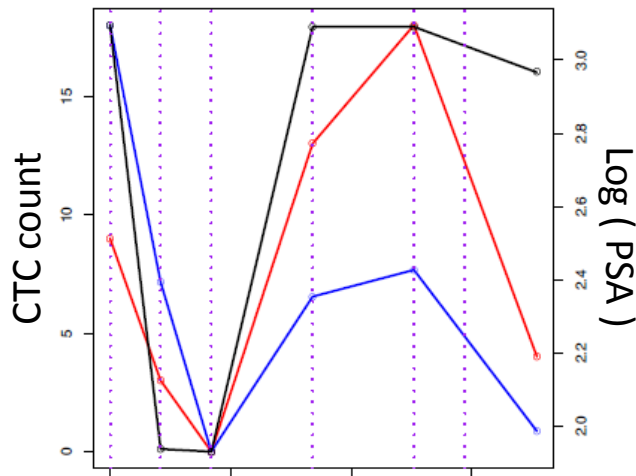
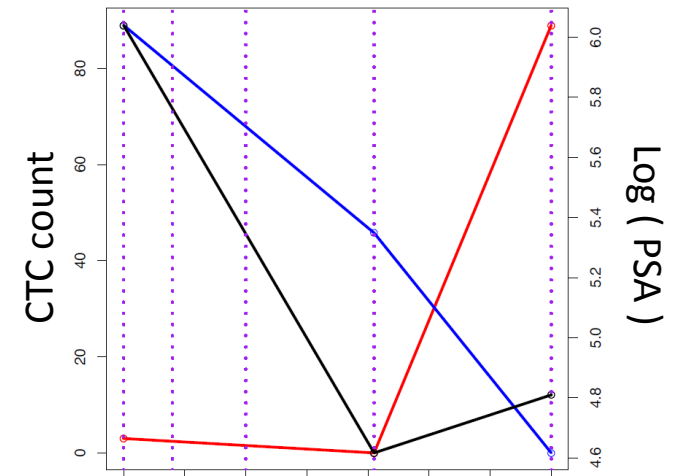


**Simulated individual kinetic profile #3**



**Simulated individual kinetic profile #4**



**Observed individual kinetic profile #1****Observed individual kinetic profile #2****Simulated individual kinetic profile #3****Simulated individual kinetic profile #4**

→ Simulations of different types of individual kinetic profiles similarly to those observed

# Parameter estimates

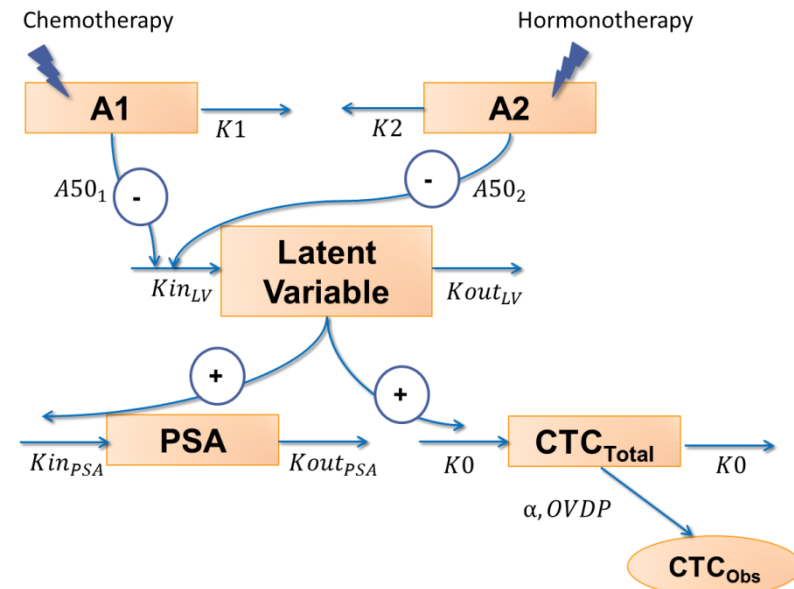
- Relative standard errors all less than 13 %  
→ **Satisfactory precision** in the estimations
- **Large inter individual variability (IIV)**  
→ Supported by the data. No available covariates.
- $Q50_{Chemo} = 0.0006 < Q50_{Hormo} = 0.04$   
→ Chemotherapy had a **greater inhibiting potency**
- PSA half-life = 98 days
- CTC lifespan = 114 days (CV=15%)

# DISCUSSION & CONCLUSIONS

# Discussion

- An **atypical model** combining several advanced features in pharmacometrics:

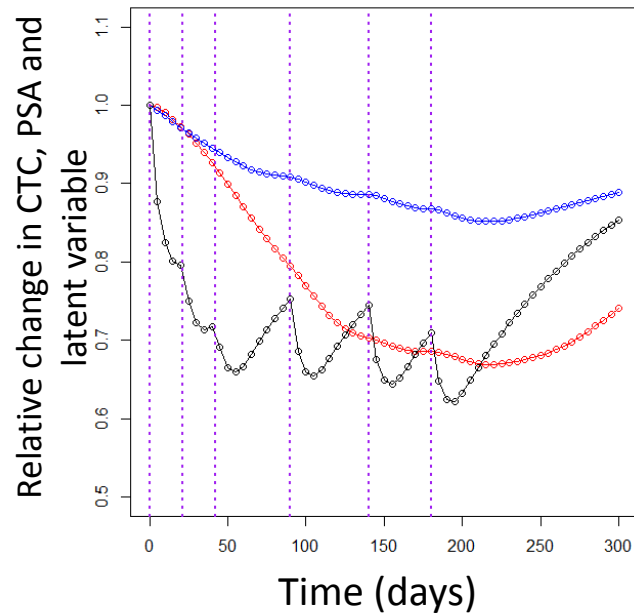
- K-PD modeling for each treatment type
- Latent variable: tumor burden producing PSA and CTC
- Joint modeling of count and continuous data
- Cell life span model
- Negative binomial distribution for the CTC random sampling process



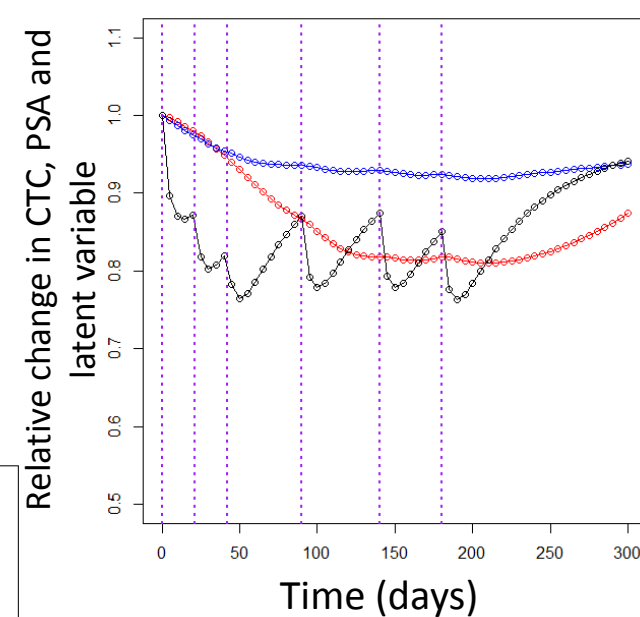
- First model quantifying the **dynamic relationships** between the kinetics of PSA and CTC count in treated mCRPC patients

# Typical simulated kinetic profiles

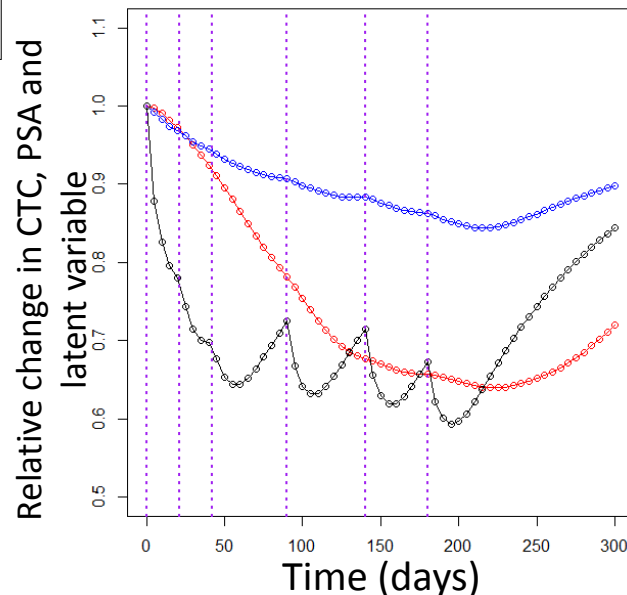
Typical patient receiving  
chemotherapy



Typical patient receiving  
hormonotherapy



Typical patient receiving  
both



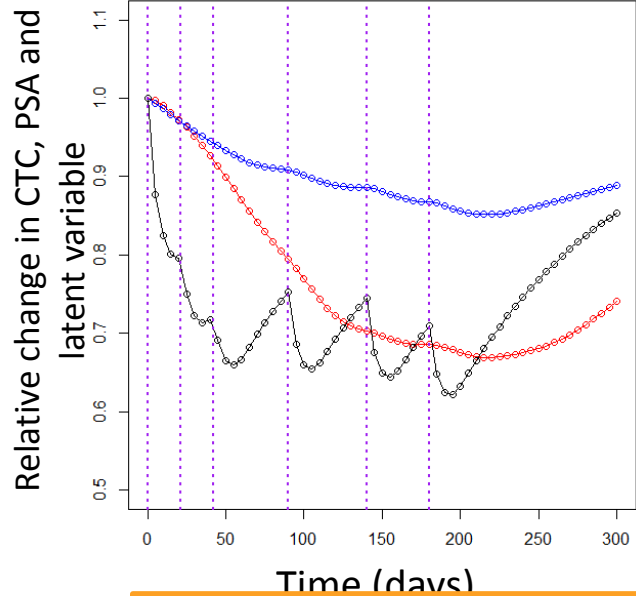
- PSA kinetics
- CTC count kinetics
- Latent variable kinetics
- ⋯ Treatment cycle



# Typical simulated kinetic profiles

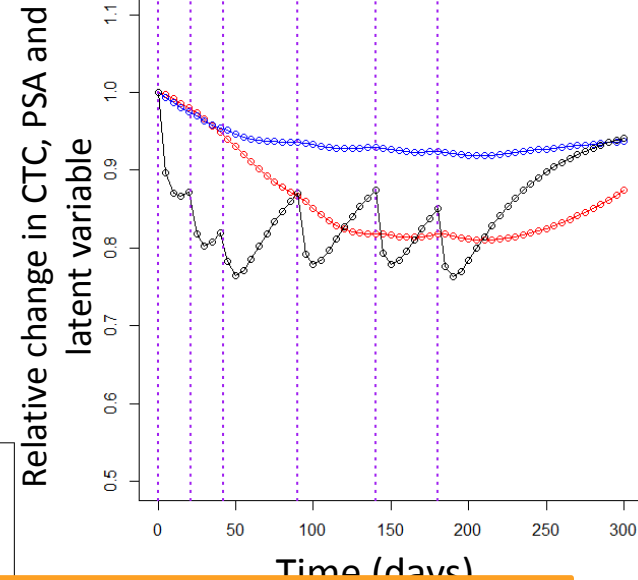
Typical patient receiving chemotherapy

Typical patient receiving hormonotherapy

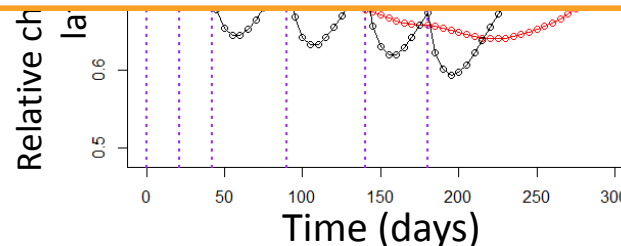


- PSA kinetics
- CTC count kinetics
- Latent variable kinetics
- ⋯ Treatment cycle

Typical patient receiving both



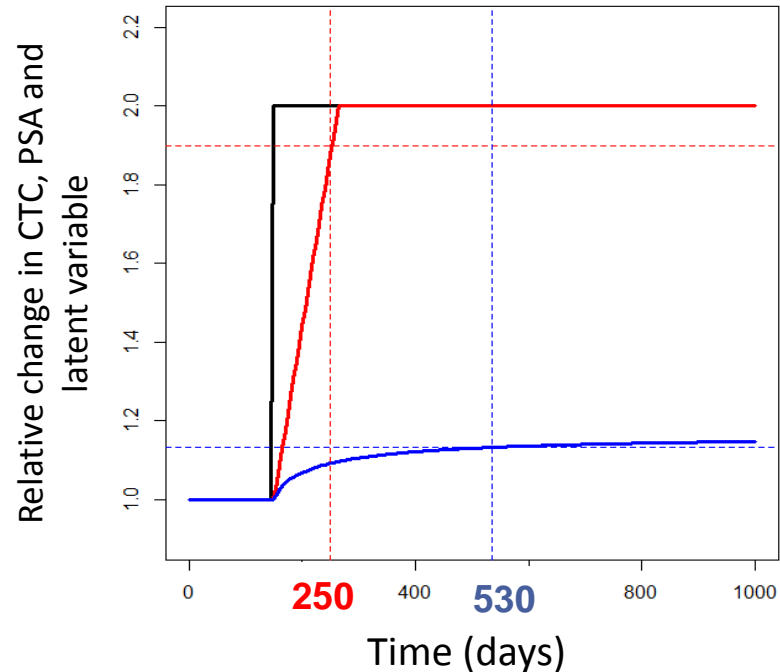
→ **CTC more sensitive** to latent variable variations compared to PSA



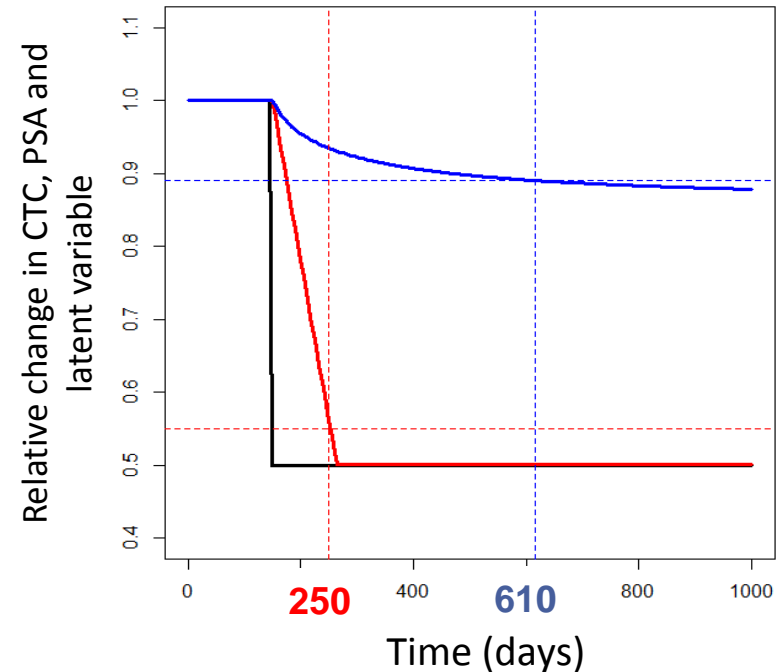
# PSA & CTC kinetics sensitivity

- Latent Variable kinetics
- PSA kinetics
- CTC count kinetics

Increased latent variable



Decreased latent variable



- **CTC more sensitive** to latent variable variations compared to PSA
- **CTC kinetics faster** than PSA kinetics

# Perspectives and Applications

- **To establish** a link between a CTC kinetic parameter and survival (OS or PFS)
- **To compare** the sensitivity and specificity of PSA and CTC count for predicting treatment efficacy
- **To identify** some covariates explaining the variability
  - **To predict treatment efficacy during drug development or for therapeutic adjustment in treated mCRPC patients**

# Thank you !



**BACKSLIDES**

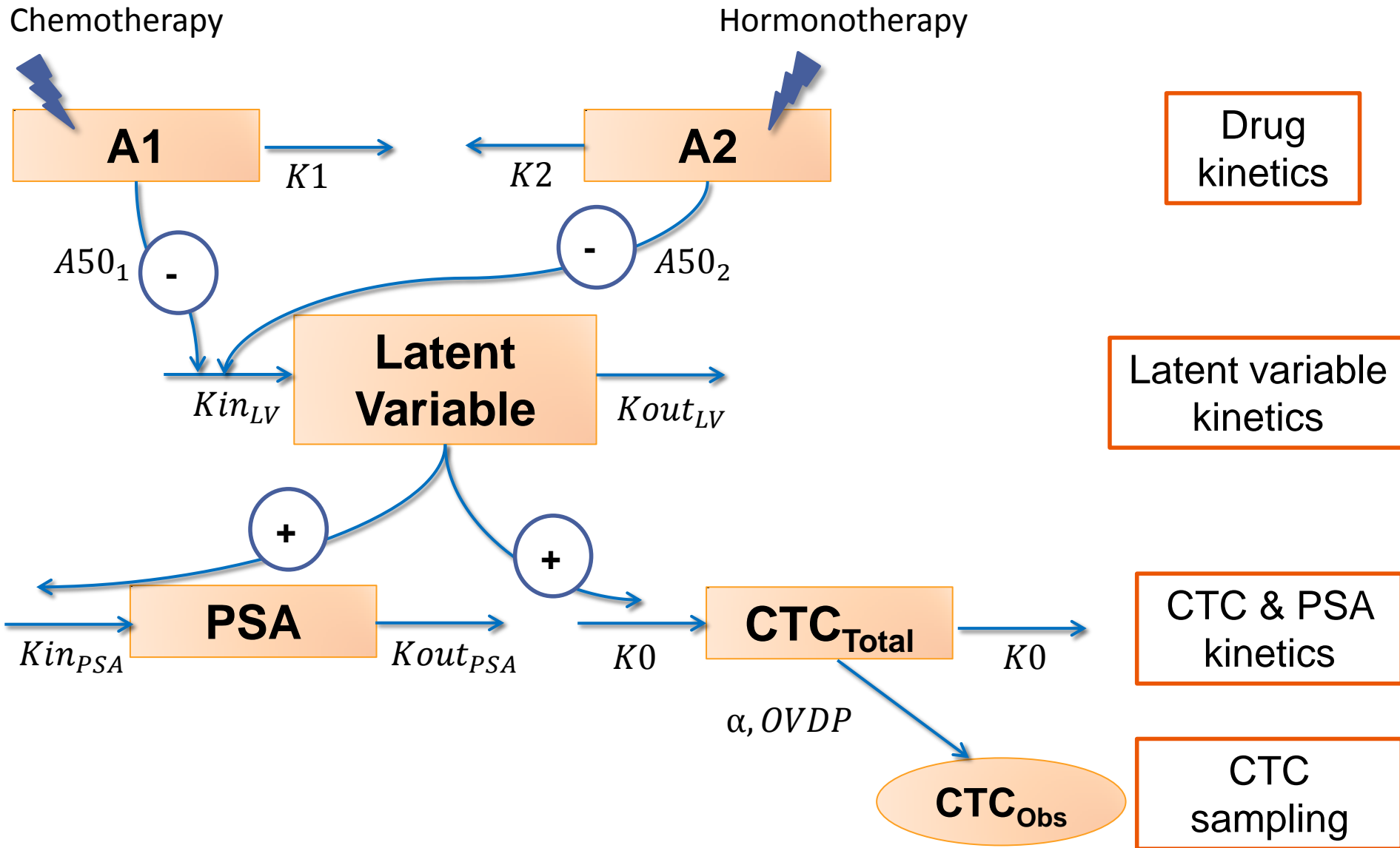
# Patient characteristics (1)

| Patient characteristics                           | Data               |
|---|--------------------|
| Number of patients                                | 223                |
| Total Number of CTC observations                  | 919                |
| CTC count value                                   | 2 [0 – 6 437]      |
| Baseline CTC count                                | 7 [0 – 5 925]      |
| Number of CTC count = 0                           | 365 (40%)          |
| Number of CTC observations per patient            | 4 [2 - 6]          |
| Total Number of PSA observations                  | 928                |
| PSA concentration (ng.mL <sup>-1</sup> )          | 116 [LOQ – 17 800] |
| Baseline PSA concentration (ng.mL <sup>-1</sup> ) | 130 [2 – 17 800]   |
| Number of BLQ values of PSA                       | 1 (0.11%)          |
| Number of PSA observation per patient             | 4 [1 - 6]          |
| Follow-up time (days)                             | 124 [21 - 177]     |
| Number of treatment cycles                        | 5 [2 - 10]         |

# Patient characteristics (2)

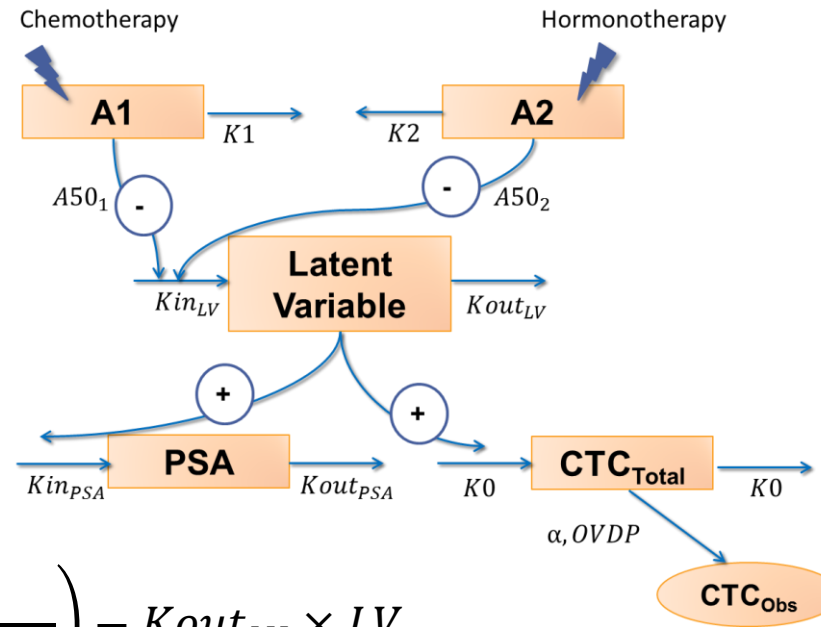
| Patient characteristics  | Data  |
|--|---|
| XRT before T0: Yes<br>No   | 142 (63%)<br>82 (37%)   |
| Radical Prostatectomy before T0: Yes<br>No   | 63 (28%)<br>161 (72%)   |
| Bisphosphonates before T0: Yes<br>No   | 15 (7%)<br>209 (93%)  |
| Corticotherapy before T0: Yes<br>No  | 48 (21%)<br>176 (79%)   |
| Ketocenazole before T0: Yes<br>No  | 44 (20%)<br>180 (80%)   |
| Type of chemotherapy at T0: Taxanes<br>Other   | 164 (73%)<br>60 (27%)   |
| Type of hormonotherapy at T0: 0<br>An GnRH<br>An GnRH + Anti andro<br>An GnRH + Oestro<br>Anti andro<br>Oestro | 45 (20.1%)<br>170 (75.9%)<br>1 (0.4%)<br>6 (2.8%)<br>1 (0.4%)<br>1 (0.4%) |
| Line of chemotherapy at T0: 1<br>2<br>>2   | 148 (66%)<br>39 (17%)<br>37 (17%)   |
| Line of hormonotherapy: 1<br>2<br>3<br>>3  | 53 (24%)<br>101 (45%)<br>42 (19%)<br>28 (12%)                             |

# Model





# Model Equations



$$\left\{ \begin{array}{l} \frac{dA1}{dt} = -K1 \times A1 \\ \frac{dA2}{dt} = -K2 \times A2 \\ \frac{dLV}{dt} = Kin_{LV} \times \left(1 - \frac{A1}{Q50_1 + A1}\right) \times \left(1 - \frac{A2}{Q50_2 + A2}\right) - Kout_{LV} \times LV \\ \frac{dPSA}{dt} = Kin_{PSA} \times LV - Kout_{PSA} \times PSA \\ \frac{dCTC_{Total}}{dt} = K0 \times LV - K0 \times CTC_{Total} \end{array} \right.$$

$$\left\{ \begin{array}{l} A1(0) = 0 \\ A2(0) = 0 \\ LV(0) = LV_0 = 1 \text{ FIX with } LV_0 < \frac{Kin_{LV}}{Kout_{LV}} \\ PSA(0) = PSA_0 \\ CTC_{Total}(0) = K0 \times LV_0 \end{array} \right.$$

# Latent Variable Condition

$$LV(0) = LV_0 \text{ with } LV_0 < \frac{Kin_{LV}}{Kout_{LV}}$$

→ To allow the latent variable to increase

→ Use of the Logit function:

$$LV_0 = \frac{Kin_{LV}}{Kout_{LV}} \times \frac{\exp(THETA + ETA)}{1 + \exp(THETA + ETA)}$$

→ Applying on KinLV:

$$Kin_{LV} = \frac{LV_0 \times Kout_{LV}}{\frac{\exp(THETA + ETA)}{1 + \exp(THETA + ETA)}}$$

# Negative Binomial Distribution

Equation:

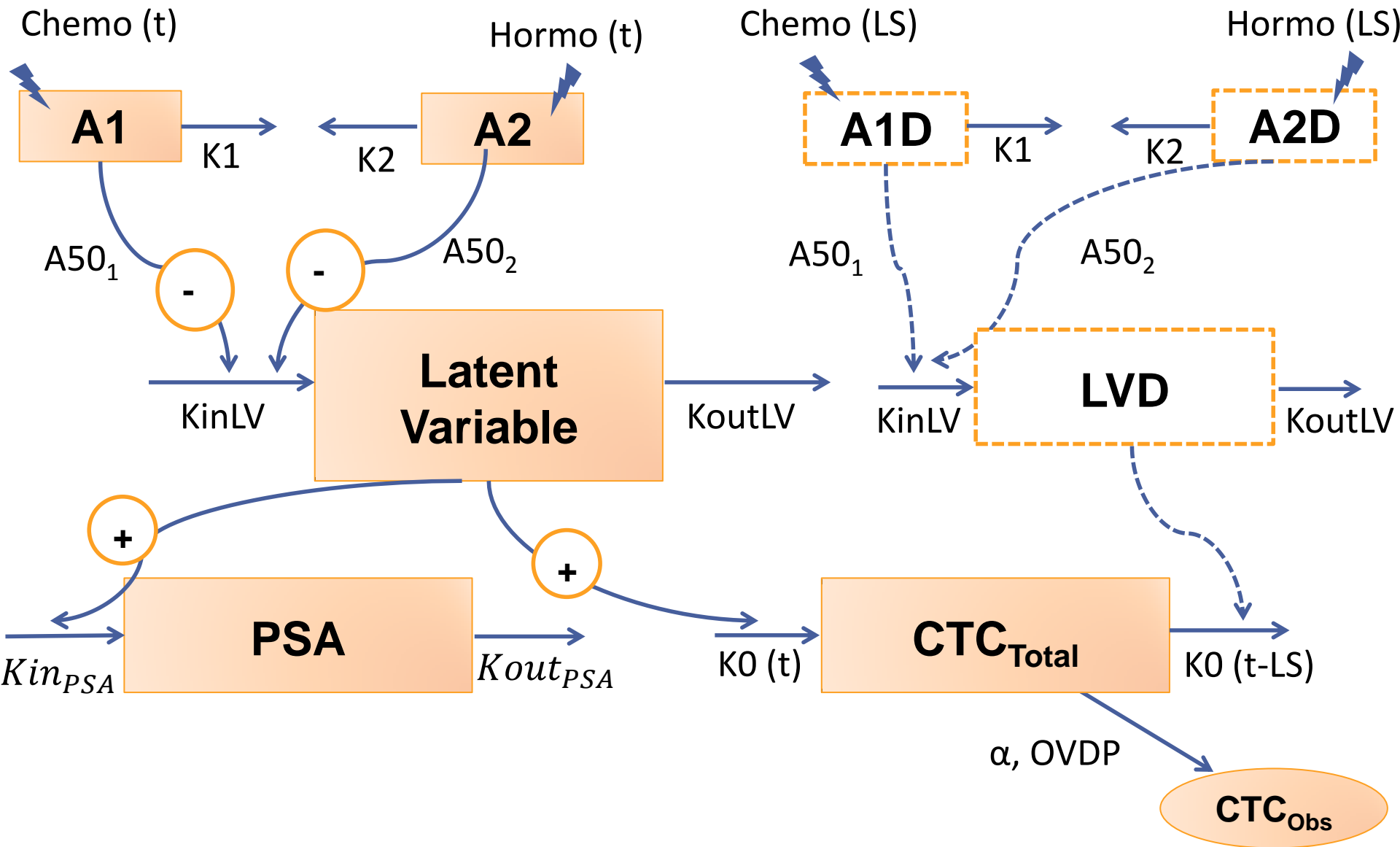
$$P(CTC_{Obs} = n) = \left[ \frac{\Gamma(n + \frac{1}{OVDP})}{n! \times \Gamma(\frac{1}{OVDP})} \right] \times \left( \frac{1}{1 + OVDP \times \lambda} \right)^{\frac{1}{OVDP}} \times \left( \frac{\lambda}{\frac{1}{OVDP} + \lambda} \right)^n$$

$\Gamma$  and  $n!$  are the Gamma and Factorial functions. OVDP is the overdispersion parameter, allowing to estimate a variance greater than the mean.

The variance of the negative binomial model is equal to:

$$Var = \lambda \times (1 + OVDP \times \lambda)$$

# Model with delayed compartments



# Model equations with delayed compartments

$$\left\{ \begin{array}{l}
 \frac{dA1}{dt} = -K1 \times A1 \\
 \frac{dA2}{dt} = -K2 \times A2 \\
 \frac{dLV}{dt} = Kin_{LV} \times \left(1 - \frac{A1}{Q50_1 + A1}\right) \times \left(1 - \frac{A2}{Q50_2 + A2}\right) - Kout_{LV} \times LV \\
 \frac{dA1D}{dt} = -K1 \times A1D \\
 \frac{dA2D}{dt} = -K2 \times A2D \\
 \frac{dLVD}{dt} = Kin_{LV} \times \left(1 - \frac{A1D}{Q50_1 + A1D}\right) \times \left(1 - \frac{A2D}{Q50_2 + A2D}\right) - Kout_{LV} \times LVD \\
 \frac{dCTC}{dt} = K0 \times LV - K0 \times LVD \\
 \frac{dPSA}{dt} = Kin_{PSA} \times LV - Kout_{PSA} \times PSA
 \end{array} \right.$$

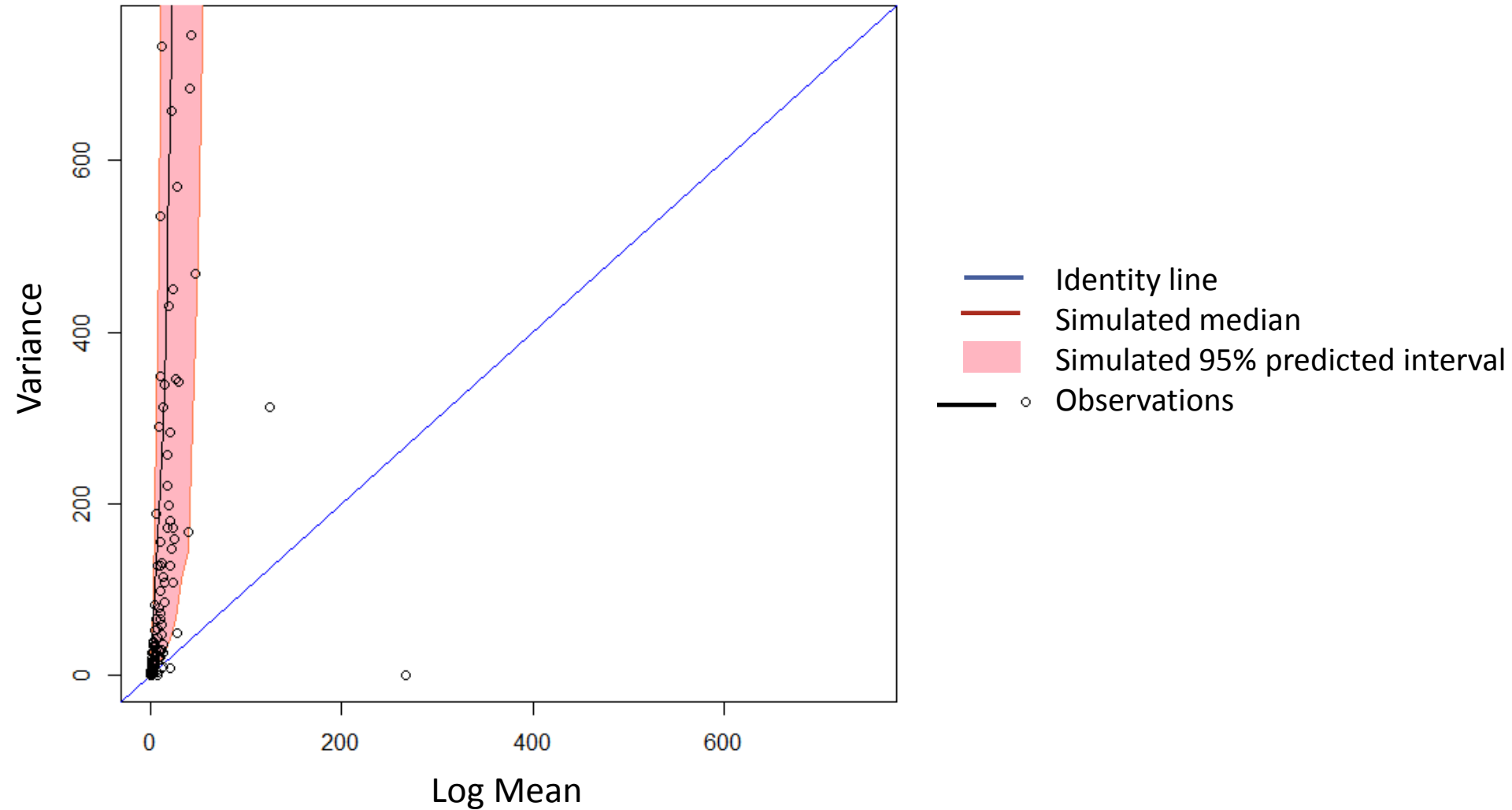
**Conditions initiales:**

$$\begin{array}{ll}
 A1(0) = 0 & A1D(0) = 0 \\
 A2(0) = 0 & A2D(0) = 0 \\
 LV(0) = LV0 = 1 \text{ FIX} & LVD(0) = LV0 \\
 F4 = K0 \times LS5 & PSA(0) = PSA0 \\
 LS6 = LS5 & \\
 LS7 = LS5 &
 \end{array}$$

# Parameter Estimates

| Part of the model  | Parameter (unit)   | Estimate | RSE Estim. (%) | IIV CV (%) | RSE IIV |
|--|--|----------|----------------|------------|---------|
| <b>Drug kinetics</b><br>1: chemotherapy<br>2: hormonotherapy | K1 (Day <sup>-1</sup> )  | 0.595    | 10             | 126        | 3       |
|  | K2 (Day <sup>-1</sup> )  | 0.456    | 8              | 114        | 3       |
|  | Q50 <sub>1</sub> (AU)  | 0.0006   | 6              | 114        | 8       |
|  | Q50 <sub>2</sub> (AU)  | 0.0433   | 11             | 105        | 1       |
| <b>Latent variable kinetics</b>                              | LV0 (AU)   | 1 FIX    | /              | 0 FIX      | /       |
|  | Kout <sub>LV</sub> (Day <sup>-1</sup> )  | 0.00734  | 13             | 204        | 13      |
|  | Kin <sub>LV</sub> (AU.day <sup>-1</sup> )                                      | 8.88     | 1              | 126        | 6       |
| <b>PSA kinetics</b>  | Kin <sub>PSA</sub> (ng.mL <sup>-1</sup> .day <sup>-1</sup> .AU <sup>-1</sup> ) | 1.04     | 5              | 155        | 5       |
|  | Kout <sub>PSA</sub> (Day <sup>-1</sup> )                                       | 0.0071   | 7              | 145        | 4       |
|  | PSA0 (ng.mL <sup>-1</sup> )  | 150      | 5              | 152        | 2       |
| <b>CTC kinetics</b>  | K0 (CTC.day <sup>-1</sup> .AU <sup>-1</sup> )                                  | 153      | 0.9            | 11         | 2       |
|  | LS (Day)   | 114      | 1              | 15         | 2       |
| <b>CTC sampling</b>  | OVDP (AU)  | 5.7      | 4              | 141        | 1       |
| <b>Residual Variab</b>                                       | PSA Residual error   | 0.3      |                | /          | /       |

# VPC Overdispersion (normal scale)



# Categorical VPCs : $\leq 5$ CTCs vs $>5$ CTCs

